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Abstract

This paper applies two recent stated choice survey datasets of Japan to investigate the difference between the latent class model (LCM) and the mixed logit model (MLM) for transport mode choice. A detailed comparison is carried out, focusing on comparing values of time savings, direct choice elasticities, predicted choice probabilities and prediction success indices. Furthermore, a test on non-nested model is also utilized to help determine which model is superior to another one. The results suggest that the LCM performs better than the MLM in both datasets.

Keywords: latent class model (LCM), mixed logit model (MLM), transport mode choice, predicted choice probability, prediction success index

JEL classification: C35, D12, R41

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1. Introduction

In the recent thirty years, analysts have made a great endeavor on developing different discrete choice models to relax the assumption of independence from irrelevant alternatives (IIA) in the fundamental multinomial logit model (MNL). Among these models, the mixed logit model (MLM) is probably the most flexible one (see, for instance, Revelt and Train, 1998; McFadden and Train, 2000; Bhat, 2003; Greene and Hensher, 2003; Bhat and Gossen, 2004, etc.). It generalizes a standard MNL by allowing its parameter associated with observed variable to vary with a known population distribution across individuals. Alternatively, the latent class model (LCM), which is frequently applied in marketing research, assumes that a discrete number of latent classes are sufficient to account for preference heterogeneity. Comparing with the mixed logit model specification, the LCM has the advantage of being relatively simple, reasonably plausible, and statistically testable. However, it is somewhat less flexible than the MLM since the parameters associated with each variable in each class are fixed. In contrast, the main disadvantage of the MLM is that the assumption made on the distributions of parameters should be specified by the analysts. Due to that each model has its virtues and limitations, it is meaningful to compare between these two advanced discrete choice models.

A recent study by Greene and Hensher (2003) compared the LCM with the MLM by using a dataset of road type's choice by car in New Zealand. After a detailed comparison on value of travel time savings, direct share elasticities, choice sensitivities to 50% increase in travel time, and choice probabilities, they concluded that although both the mixed logit and latent class models offer attractive specifications than the multinomial logit, it is inconclusive that which one is 'completely' superior to another despite some stronger statistical evidences support for the latent class model in their dataset.¹ Remained as a future study implication, they mentioned that "we encourage a greater effort to compare and contrast such advanced models as one approach to searching for rules on stability in explanation and prediction" (Greene and Hensher 2003).

Strongly encouraged by their study, we will use two stated preference datasets of transport modal choice (monorail, car and bus) in Japan to make a comparison between the MLM and the LCM. Thus, the prime purpose of this paper is to seek for whether or not the results of the comparison suggest that the latent class model is to some extent superior to the mixed logit model as Greene and Hensher (2003) mentioned in their study.

¹ The inconclusiveness is due to the reason that these two models are non-nested, therefore, normal Likelihood Ratio (LR) test can not be applied.

The rest of the paper is organized as follows. Section 2 provides a brief introduction on the latent class and the mixed logit models. Section 3 compactly describes our two stated preference datasets in Japan. Section 4 presents a comparison between these two models, and Section 5 draws conclusions of the paper.

2. The latent class and mixed logit models²

2.1 The latent class model

The latent class model, unlike the MLM which specifies the random parameters to follow a continuous joint distribution, assumes that a discrete number of classes are sufficient to account for preference heterogeneity across classes. Therefore, the unobserved heterogeneity is captured by these latent classes in the population, each of which is associated with a different parameter vector in the corresponding utility. The LCM has often been used in marketing research instead of ML model, while there are few studies in other fields such as transportation.

The choice probability that individual q of class s chooses alternative i from a particular set J, which is comprised of j alternatives, is expressed as:

$$P_{iq|s} = \exp(\beta'_{s} X_{iq}) / \sum_{j=1}^{J} \exp(\beta'_{s} X_{jq}) \quad s = 1, ..., S$$
(1)

where β'_{s} is the parameter vector associated with the vector of explanatory variables X_{iq} . Note that Eq. (1) is a simple MNL specification in class *s*.

Additionally, one can construct a classification model as a function of some individual-specific attributes to explain the heterogeneity across classes. The LCM model simultaneously estimates Eq. (1) for S classes and predicts the probability H_{qs} as individual q being in class s. Then, the unconditional probability of choosing alternative i is given as:

$$P_{iq} = \sum_{s=1}^{5} P_{iq|s} H_{qs}$$
(2)

An issue to be noted is the choice of *S*, the number of classes. Since this is not a parameter, hypotheses on *S* cannot be tested directly. However, as Louviere *et al.* (2000, chap. 10) mentioned that a number of methods to decide *S* have been used based on the Akaike Information Criterion (AIC) and its variants. AIC and Consistent AIC (CAIC), which are given in Eqs. (3) and (4), are used to guide model selection.

² Since Greene and Hensher (2003) have provided a detail description on the latent class model and the mixed logit model, therefore, we just give a brief introduction on these two models. For the other literature on the MLM and LCM, see Revelt and Train (1998), Louviere *et al.* (2000), McFadden and Train (2000), Bhat and Gossen (2004), etc.

$$AIC = -2(LL(\hat{\beta}) - S \cdot K_s - (S - 1)K_c)$$
⁽³⁾

$$CAIC = -2LL(\hat{\beta}) - (S \cdot K_s + (S - 1)K_c - 1)(\ln(2N) + 1)$$
(4)

where $LL(\hat{\theta})$ is the log likelihood at the estimated parameters $\hat{\beta}$, K_s is the number of elements in the utility function of the class-specific choice models, K_c is the total number of parameters in the classification model, and N is the number of observations in the sample. The value of S that minimizes each of the measures of AIC and CAIC suggests which model should be preferred (Louviere *et al.* 2000, chap. 10).

2.2 The mixed logit model

The mixed logit model allows for a heightened level of flexibility by specifying taste coefficients to be randomly distributed across individuals. Additionally, superior to LCM, MLM can account for potential correlation over repeated choices made by each individual by imposing a first-order autoregressive (AR1) process³.

The model is a generalization of the MNL model, summarized as below:

$$P_{iqt} = \exp(\alpha' + \beta' X_{iqt} + \varphi' F_{iqt}) / \sum_{j=1}^{J} \exp(\alpha' + \beta' X_{jqt} + \varphi' F_{jqt})$$
(5)

where

- α' is a vector of fixed or random alternative-specific constants (ASCs) associated with i = 1,..., J alternatives and q = 1,..., Q individuals, and one of these ASCs should be identified as 0.
- β' is a parameter vector that is randomly distributed across individuals.
- φ' is a vector of non-random parameters.
- *X_{iqt}* is a vector of individual-specific characteristics and alternative-specific attributes at observation *t*, and is estimated with random parameters.
- F_{iqt} is a vector of individual-specific characteristics and alternative-specific attributes at observation *t*, and is estimated with fixed parameters.

In this specification, a subset or all of α' and the parameters in the β' vector can be assumed to be randomly distributed across individuals⁴. These random parameters can then be defined as a function of characteristics of individuals and/or other attributes that are choice invariant. Based on these defined attributes, the mean

 $^{^3}$ Greene and Hensher (2003) mentioned that the latent class model does not readily extend to autocorrelation, therefore, this aspect is left for future research.

⁴ The distributions of random parameters can be considered, for example, normal distribution, lognormal distribution, and triangular distribution, etc.

and standard deviations of specified random parameters and contributions from these choice invariant attributes to random parameters are estimated by using Maximum Simulated Likelihood (MSL) method. The MLM is sufficiently flexible that it provides the modeler a tremendous range to specify individual unobserved heterogeneity. To some extent, this flexibility offsets the specificity of the distributional assumptions (Greene and Hensher 2003).

3. Data

We use two survey datasets, which are recently collected in Osaka of Japan, to compare the LCM with the MLM. The first survey is based on a stated choice experiment carried out in July 2005 on transport mode choices by the residents in the Saito and Onohara Area of Northern Osaka (hereinafter, called Saito survey). A prime purpose of this experiment is to investigate whether or not individual environmental consciousness is one of the determinants in transport modal choice. The transport modes in the choice set faced by each respondent consist of monorail, car and bus. This dataset is composed of 467 individuals with each answering 8 choice sets, therefore, the total observations are 3736 (i.e. 467*8 observations). Five attributes are used in the stated choice experiment as follows.

- A. In-vehicle time including delay time caused by traffic jam (in minutes)
- B. Access time (in minutes)
- C. Frequency (in minutes)
- D. Travel cost (in JP yen)
- E. Negative impact on the environment caused by transport modes

For each attribute, we adopted a 2-level design expect for access time and frequency in car and negative impact on the environment in monorail. Then, 32 choice sets were constructed by a fractional factorial design to reduce the number of choice sets to a manageable level. These 32 choice sets were further blocked into 4 versions avoiding a dominant selection. Each sampled individual was asked to answer one version. An example of the choice sets is provided in Table 1. Further details on the survey are given in Shen *et al.* (2005).

The second dataset is based on another stated choice survey on transport mode choice of the residents in Eastern Osaka (hereinafter, called Eastern Osaka survey), which was also carried out in July 2005. Different from the first one, this survey focused

Table 1 An example of choice set in Saito survey

| | Monorail | Car | Bus |
|---|----------|------------------------|--------------------------|
| In-vehicle time including delay time caused by traffic jam (minutes) | 15 | 40 | 50 |
| Access time (minutes) | 15 | almost 0 | 3 |
| Frequency (minutes) | 10 | at any time | 15 |
| Generalized cost (JP yen) | 360 | 800 | 280 |
| Negative impact on the environment (such as CO ₂ emission) | Low | 3 times as monorail | 2.5 times as monorail |
| Please choose one most preferable transport mode and \checkmark in \Box | | | |

Table 2 An example of choice set in Eastern Osaka survey

| | Monorail | Car | Bus |
|---|---------------|---------------|---------------|
| Average in-vehicle time for 1 section (minutes) | 3 | 4 | 10 |
| Average delay time due to congestion (minutes) | 0 | 8 | 10 |
| Average cost (JP yen) | 100 | 200 | 60 |
| Frequency (numbers/hour) | 4 | at any time | 10 |
| Local natural environment | Worse than | Worse than | Worse than |
| | current state | current state | current state |
| Network accessibility | Only monorail | Only monorail | Only monorail |
| Please choose one most preferable transport mode and \checkmark in \Box | | | |

on both impacts of local natural environment and network accessibility on transport modal choice. Same experimental design strategy as that in Saito survey was used, except that the local natural environment and network accessibility were treated as a common condition in each choice set, i.e. they were allowed to vary across choice sets but not across alternatives. A total of 453 valid responses, each with 8 choice sets, produce 3624 observations (i.e. 453*8 observations). Table 2 shows an example of the choice sets, and Sakata *et al.* (2005) provides further details on this survey.

4. A comparison between LCM and MLM

Tables 3 and 4 summarize the estimated results of the two datasets with the specifications of MNL, MLM and LCM⁵. We have specified a number of individual socio-economic characteristics and added them into the estimated model. However, to save space, we omit these results in the tables.

With respect to the mixed logit model, we have defined all time-associated attributes as random parameters and selected a Normal distribution for them. Specifying a given parameter to follow a Normal distribution is equivalent to making a priori assumption that both positive and negative values for this parameter may exist in the population. Concerning the possible positive signs of time-associated parameters, Hess et al. (2005) have noted that "a negative measure for VTTS [value of travel time savings] for a given individual in effect suggests that this individual would be willing to pay for increases in travel-time. At first sight, this is counter-intuitive. However, several recent papers discuss zero (Richardson, 2003) or positive (Redmond and Mokhtarian, 2001) elasticity with respect to travel-time. There are interesting statements like: 'I'd rather have an hour-plus commute than a five-minute commute. In the morning, it gives me a chance to work through what I'm going to do for the day. And it's my decompression time.'(Sipress, 1999, cited by Redmond and Mokhtarian, 2001)". This citation indicates that if an individual is more satisfied with longer time-associated attributes due to some individual-specific reasons, the positive sign of time-associated attributes could be possible.⁶

Akaike Information Criterion (AIC) and Consistent AIC (CAIC) given in Eqs. (3) and (4) were used to select the number of classes in the latent class model. As a result, both AIC and CAIC were the lowest ones in three latent classes for both datasets. Therefore, three-class LCMs were estimated for both Saito and Eastern Osaka surveys. From the results in Tables 3 and 4, based on the log likelihood values, the hypothesis that the MNL model is in favor of either the MLM or the LCM can be safely rejected.

With respect to the comparison between MLM and LCM, we focus on contrasting

⁵ All the results were estimated by NLOGIT 3.0 (Econometric Software, Inc., 2003).

⁶ We have also estimated the MLM with a specification of triangular distribution on time-associated parameters. However, we did not find large differences between normal distribution and triangular distribution specifications on the estimated parameters, value of time savings, and choice elasticities, etc.

| Attribute | Alternative | MNL | MLM | | LCM | |
|------------------------|-------------|-----------|-----------|---------|-----------|----------|
| | | | | Class 1 | Class 2 | Class 3 |
| In-vehicle time | All | -0.0758 | -0.1668 | -0.0653 | -0.1160 | -0.0858 |
| | | (-25.45) | (-17.12) | (-4.05) | (-36.34) | (-11.47) |
| Access time | All | -0.0265 | -0.0575 | -0.0270 | -0.0642 | -0.0088 |
| | | (-2.08) | (-2.59) | (-3.78) | (-3.48) | (-2.94) |
| Frequency | All | -0.0155 | -0.0247 | -0.0228 | -0.0232 | -0.0097 |
| | | (-3.57) | (-3.21) | (-2.04) | (-4.63) | (-2.82) |
| Travel cost | All | -0.0027 | -0.0049 | -0.0019 | -0.0056 | -0.0014 |
| | | (-9.87) | (-10.13) | (-3.30) | (-15.42) | (-3.50) |
| Negative environmental | All | -0.7066 | -0.5100 | -3.1898 | 0.3882 | -3.1662 |
| impact | | (-2.78) | (-3.06) | (-2.52) | (1.273) | (5-5.97) |
| Monorail constant | Monorail | -0.7612 | -1.7252 | 19.3000 | -2.0457 | 0.9842 |
| | | (-3.19) | (-3.22) | (0.02) | (-7.90) | (1.71) |
| Car constant | Car | -1.3935 | -3.4679 | 0.4838 | -18.5697 | 4.1862 |
| | | (-4.41) | (-4.92) | (0.00) | (-0.02) | (5.48) |
| In-vehicle time | All | | 0.1039 | | | |
| standard derivation | | | (11.17) | | | |
| Access time | All | | 0.2109 | | | |
| standard derivation | | | (14.79) | | | |
| Frequency | All | | 0.0848 | | | |
| standard derivation | | | (12.12) | | | |
| Latent Class | | | | 0.14175 | 0.58520 | 0.27305 |
| probability | | | | (7.15) | (20.30) | (10.781) |
| Log-likelihood | | -2853.062 | -2320.686 | | -1954.913 | |
| Pseudo- R^2 | | 0.1844 | 0.3366 | | 0.4460 | |

 Table 3

 Estimated results for Saito survey (*t* statistics in parentheses)

indicators of willingness to pay, e.g. values of time savings, choice elasticities, predicted choice probabilities of each transport mode, and prediction success index, respectively. In addition, a test on non-nested choice models which is based on the AIC proposed by Ben-Akiva and Swait (1986) is applied to help determine which model is relatively more superior in the two datasets applied in this study.

Tables 5 and 6 summarize the estimated values of time savings (VOTS). For both datasets, the mean estimates of VOTS by the MLM specification differ substantially with the three latent classes for LCM, although in Saito survey, VOTS of in-vehicle time is similar to that in class 1 and VOTS of access time is similar to that in class 2. Overall,

| Attribute | Alternative | MNL | MLM | LCM | | |
|-----------------------|-------------|-----------|-----------|----------|-----------|---------|
| | | | | Class 1 | Class 2 | Class 3 |
| In-vehicle time | All | -0.1251 | -0.2669 | -0.1365 | -0.2825 | -0.1915 |
| | | (-8.65) | (-10.23) | (-5.51) | (-8.62) | (-3.55) |
| Delay time | All | -0.0606 | -0.1338 | -0.0672 | -0.1522 | -0.0501 |
| | | (-8.10) | (-8.94) | (-5.10) | (-10.36) | (-2.10) |
| Frequency | All | -0.0328 | -0.1101 | -0.0710 | -0.0913 | -0.0377 |
| | | (-3.18) | (-8.67) | (-3.97) | (-5.94) | (-2.21) |
| Travel cost | All | -0.0050 | -0.0083 | -0.0157 | -0.0062 | -0.0022 |
| | | (-13.29) | (-15.52) | (-13.19) | (-10.70) | (-2.55) |
| Monorail constant | Monorail | 1.3564 | 2.0211 | 1.0647 | 2.1905 | -0.1073 |
| | | (7.25) | (7.04) | (2.42) | (6.64) | (-0.18) |
| Bus constant | Bus | 0.3930 | 0.9844 | 0.6429 | 0.3326 | -1.3832 |
| | | (1.95) | (3.43) | (1.43) | (0.77) | (-1.54) |
| Local natural | Monorail | 0.4150 | 0.4396 | -0.9100 | 0.9895 | 1.3309 |
| environment | | (1.85) | (2.19) | (-1.55) | (2.74) | (2.24) |
| Network accessibility | Monorail | 0.7705 | 0.9924 | 0.7249 | 1.2860 | 1.5493 |
| | | (3.33) | (2.60) | (1.16) | (3.66) | (2.44) |
| Local natural | Bus | 0.2396 | 0.1647 | -0.9972 | -0.1079 | -5.9485 |
| environment | | (0.87) | (0.42) | (-1.70) | (-0.14) | (-1.61) |
| Network accessibility | Bus | 0.7990 | 1.0638 | 0.8712 | -0.1265 | 5.8119 |
| | | (2.91) | (2.60) | (1.40) | (-0.16) | (4.48) |
| In-vehicle time | All | | 0.2799 | | | |
| standard derivation | | | (12.16) | | | |
| Delay time | All | | 0.1620 | | | |
| standard derivation | | | (9.95) | | | |
| Frequency | All | | 0.1993 | | | |
| standard derivation | | | (14.37) | | | |
| Latent Class | | | | 0.35625 | 0.52661 | 0.11714 |
| probability | | | | (12.60) | (18.02) | (6.43) |
| Log-likelihood | | -2791.523 | -2390.553 | | -1714.392 | |
| Pseudo- R^2 | | 0.0892 | 0.2200 | | 0.4406 | |

 Table 4

 Estimated results for Eastern Osaka survey (*t* statistics in parentheses)

the results from the latent class model indicate the fact that for either in-vehicle time, access time and frequency in Saito survey or in-vehicle time, delay time and frequency in Eastern Osaka survey, three segments of low, medium and high VOTS can be found. This evidence supports the claim in Greene and Hensher's (2003) study that the latent

| Table 5 |
|---|
| Values of time savings for Saito survey (JP yen per hour) |

| Time type | MNL | MLM | LCM | | |
|-----------------|------|--------|---------|---------|---------|
| | | (mean) | Class 1 | Class 2 | Class 3 |
| In-vehicle time | 1684 | 2042 | 2062 | 1243 | 3677 |
| Access time | 589 | 704 | 853 | 688 | 377 |
| Frequency | 344 | 302 | 720 | 249 | 416 |

| Table 6 |
|---|
| Values of time savings for Eastern Osaka survey (JP yen per hour) |

| Time type | MNL | MLM | LCM | | |
|-----------------|------|--------|---------|---------|---------|
| | | (mean) | Class 1 | Class 2 | Class 3 |
| In-vehicle time | 1501 | 1929 | 522 | 2734 | 5223 |
| Delay time | 727 | 967 | 257 | 1473 | 1366 |
| Frequency | 394 | 795 | 271 | 884 | 1028 |

influences are to some extent related to an individual's VOTS.

Summaries of the probability weighted choice elasticities for common attributes (in-vehicle time and travel cost) in two surveys are provided in Tables 7 and 8. The choice elasticities differ substantially between the MLM and the LCM, especially in Eastern Osaka survey. For response to changes in in-vehicle time, the LCM suggests less sensitivity for monorail and car but more sensitivity for bus than the MLM in both datasets, whilst the magnitude of sensitivity is relatively larger in Saito survey. With respect to changes in travel cost, the MLM predicts less sensitive response for almost all the modes than the LCM in both datasets with the exception of car in Eastern Osaka survey.

A comparison of predicted choice probability between the LCM and the MLM for two surveys starts from the kernel density estimators of their ratios for each mode that are listed in Figures 1 and 2. From these figures, we may find that for both datasets, the distribution around 1 is skewed to the right for monorail and to the left for car and bus.

| Time type | MNL | MLM | LCM | | | |
|-----------------|--------|--------|--------|--|--|--|
| In-vehicle time | | | | | | |
| Monorail | -0.510 | -0.586 | -0.446 | | | |
| Car | -1.304 | -1.367 | -1.361 | | | |
| Bus | -1.418 | -1.343 | -1.374 | | | |
| Travel cost | | | | | | |
| Monorail | -0.397 | -0.400 | -0.423 | | | |
| Car | -0.955 | -1.001 | -1.056 | | | |
| Bus | -0.375 | -0.398 | -0.455 | | | |

 Table 7

 Direct choice elasticities for Saito survey (probability weighted)

Table 8

Direct choice elasticities for Eastern Osaka survey (probability weighted)

| Time type | MNL | MLM | LCM | |
|-----------------|--------|--------|--------|--|
| In-vehicle time | | | | |
| Monorail | -0.181 | -0.237 | -0.179 | |
| Car | -0.276 | -0.398 | -0.306 | |
| Bus | -0.676 | -0.666 | -0.776 | |
| Travel cost | | | | |
| Monorail | -0.243 | -0.263 | -0.313 | |
| Car | -0.993 | -0.988 | -0.869 | |
| Bus | -0.331 | -0.419 | -0.785 | |
| | | | | |

This evidence indicates that at the individual level, the choice probability of monorail predicted by the LCM is relatively larger than that predicted by the MLM, whilst the choice probabilities of car and bus are relatively smaller than those predicted by the MLM. It is consistent to the result at the aggregate choice probability level for the sampled population. The respective aggregate probabilities for monorail, car and bus are in Saito survey LCM: 0.6784, 0.1881, 0.1335 and MLM: 0.6586, 0.1889, 0.1525, and

Figure 1 Kernel density estimate for probability ratio of LCM to MLM in Saito survey



Figure 2 Kernel density estimate for probability ratio of LCM to MLM in Eastern Osaka survey



Table 9 OLS regressions of predicted probability estimated by the LCM and MLM

| | Saito survey | | Ea | Eastern Osaka survey | | |
|----------|--------------|----------|---------|----------------------|----------|----------|
| | Monorail | Car | Bus | Monorail | Car | Bus |
| Constant | -0.03118 | -0.01796 | -0.0473 | -0.1205 | -0.03407 | -0.04991 |
| P_MLM | 1.132968 | 1.012928 | 1.07295 | 1.253378 | 1.175096 | 1.046462 |
| R^2 | 0.395 | 0.448 | 0.456 | 0.384 | 0.340 | 0.277 |

Note: Dependant variable is P_LCM. All the parameters are significant at 99.9% level.

Table 10Prediction success indices for Saito and Eastern Osaka surveys

| | MNL | MLM | LCM |
|----------------------|--------|--------|--------|
| Saito survey | 0.1049 | 0.1440 | 0.3259 |
| Eastern Osaka survey | 0.0435 | 0.0622 | 0.2218 |

in Eastern Osaka survey LCM: 0.5759, 0.1216, 0.3025 and MLM: 0.5369, 0.1456, 0.3175.

OLS regressions are further applied to investigate the relationship between the LCM probability and the MLM probability. The results of OLS regressions are provided in Table 9. From the relatively low R^2 for OLS regression, we may conclude that the relationship between the predicted choice probabilities under the LCM (for three latent classes) and the MLM (a normal distribution on the random parameters) is relatively weak at the individual level.

The prediction success indices suggested by McFadden (1979) are calculated and summarized in Table 10. From these indices, we found that in both datasets the LCM has more predictive capability than the MLM.

Finally, we apply a test on non-nested choice models which is based on the AIC proposed by Ben-Akiva and Swait (1986). The test is carried out as follows. Suppose there are two non-nested models 1 and 2. Model 1 explains choices using K_1 variables, while model 2 explains the same choices using K_2 variables. Assume that $K_1 \ge K_2$ and

either the two models have different functional forms or the two sets of variables are different by at least one element. Define the fitness measure for model j, j=1, 2:

$$\phi_j^2 = 1 - \frac{L_j - K_j}{L(0)}$$
(6)

where L_j is the log likelihood at convergence for model j and L(0) is the log likelihood for constants only. Ben-Akiva and Swait (1986) show that under the null hypothesis that model 2 is the true model, the probability that the fitness measure in Eq. (6) for model 1 will be greater than that of model 2 is asymptotically bounded by a function given in Eq. (7):

$$\Pr(|\rho_2^2 - \rho_1^2| \ge Z) \le \Phi(-\sqrt{-2ZL(0) + (K_1 - K_2)})$$
(7)

where Z is the difference of the fitness measures between model 1 and model 2 and assumed larger than zero, Φ is the standard normal Cumulative Distribution Function (CDF). Therefore, Eq. (7) sets an upper bound for the probability that one incorrectly selects model 1 as the true model although model 2 is the true model.

Using the above definition, we calculate that the probabilities in Eq. (7) for Saito survey and Eastern Osaka survey are $P \le \Phi(-27.039) \approx 0$ and $P \le \Phi(-36.773) \approx 0$ respectively, assuming that the MLM is model 1 and the LCM is model 2. Therefore, we may conclude that in both datasets to which we applied the test, the LCM is superior to the MLM.

5. Conclusions

This paper provides a detail comparison between two advanced specifications of discrete choice model, i.e. a latent class model and a mixed logit model. Following the study of Greene and Hensher (2003), the paper compares the values of time savings, direct choice elasticities, and predicted choice probability derived from these two models. In addition, the prediction success indices and a non-nested model test are further applied to investigate the difference between these two models, while these results indicate that the LCM performs statistically better than the MLM in our two datasets.

Although our results are consistent with that one concluded from Greene and Hensher (2003), which claims that the latent class model is supported by stronger statistical behaviors than the mixed logit model in their dataset, we still can not make this evidence as a conclusive suggestion that the LCM is definitely superior to the MLM in all cases. More and more studies on comparison between these two specifications should be appreciated in the future, since either a systematical meta-analysis or Monte Carlo simulation can be, only after a number of accumulated studies, considered to seek for some rules on concluding which model specification is better or not.

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References

- Ben-Akiva, M. E. and Swait, J. D. (1986), "The akaike likelihood ratio index". *Transportation Science* 20(2): 133-136.
- Bhat, C. R. (2001), "Quasi-random maximum simulated likelihood estimation of the mixed logit model". *Transportation Research Part B* 35: 677-693.
- Bhat, C. R. (2003), "Simulation estimation of mixed discrete choice models using randomized and scrambled Halton sequences". *Transportation Research Part B* 37: 837-855.
- Bhat, C. R. and Gossen, R. (2004), "A mixed multinomial logit model analysis of weekend recreational episode type choice". *Transportation Research Part B* 38: 767-787.
- Bishop, R. C. and Provencher, B. (2004). "Does accounting for preference heterogeneity improve the forecasting of a random utility model? A case study". *Journal of Environmental Economics and Management* 48: 793-810
- Greene, W. H. (2003), *Econometric analysis*, Fifth edition by Pearson Education International, New York University.
- Greene, W. H. and Hensher, D. A. (2003), "A latent class model for discrete choice analysis: contrasts with mixed logit". *Transportation Research Part B* 37: 681-698.
- Hensher, D. A., Rose, J. M. and Greene, W. H. (2005). *Applied choice analysis: a primer*. Cambridge University Press, New York.
- Hess, S., Bierlaire, M. and Polak, J. W. (2005), "Estimation of value of travel-time saving using mixed logit models". *Transportation Research Part A* 39: 221-236
- Louviere, J. J., Hensher, D. A. and Swait, J. D. (2000), *Stated choice methods: analysis and applications*, Cambridge University Press.
- Maddala, G. S. (1983), Limited-dependent and qualitative variables in econometrics,

Cambridge University Press.

- McFadden, D. (1974), *Conditional logit analysis of quanlitative choice behavior*, Zarembka P. (ed.), Frontiers in econometrics, New York: Academic Press. 105-142.
- McFadden, D. (1979). "Quantitative methods for analyzing travel behavior of individuals: some recent developments". In Hensher D. A. and Stopher P. R. (eds.), *Behavioral travel modeling*, London: Croom Helm.
- McFadden, D. and Train, K. (2000), "Mixed MNL models for discrete response". *Journal* of *Applied Econometrics* 15: 447-470.
- Revelt, D. and Train, K. (1998), "Incentives for appliance efficiency in a competitive energy environment: random parameters logit models of households' choices". *Review of Economics and Statistics* 80(4): 647-657.
- Sakata, Y., Shen, J. Y. and Hashimoto, Y. (2006). "The influence of environmental deterioration and network improvement on transport mode choice". *Working Paper in Economics and Business 06-04, Graduate School of Economics and Osaka School of International Public Policy (OSIPP), Osaka University.*
- Shen, J. Y. (2005). "A Review of Stated Choice Method". *International Public Policy Studies* 10(2). *Forthcoming.*
- Shen, J. Y., Sakata, Y. and Hashimoto, Y. (2005). "Is individual environmental consciousness one of the determinants in transport mode choice". *Working Paper in Economics and Business 05-29, Graduate School of Economics and Osaka School of International Public Policy (OSIPP), Osaka University.*
- Train, K. (2003). *Discrete choice methods with simulation*. Cambridge University Press, New York.
- Train, K. and Sandor, Z. (2004). "Quasi-random simulation of discrete choice models". *Transportation Research Part B* 38: 313-327.
- Viton, P. A. (2004). "Will mixed logit change urban transport policies?". *Journal of Transport Economics and Policy* 38(3): 403-423.