## 

July 10, 2013

## Instruction to students

- 1. Dead line for submission: **July 17**, **2013**. Please submit your answer at the end of the class.
- 2. Use A4 size papers to answer.
- 3. The answer may be written in Japanese as well as English.

 $\mathbf{Q}$ 

Let  $\{Y_t\}$   $(t=1,\ldots,n)$  be an independent random sequence with

$$\mathrm{E}(Y_t) = \mu, \quad \mathrm{Var}(Y_t) = \sigma_t^2 < \infty.$$

And let be

$$\lim_{n\to\infty}\frac{1}{n}\sum_{t=1}^n\sigma_t^2=c<\infty.$$

Prove

$$\bar{Y}_n \equiv \frac{1}{n} \sum_{t=1}^n Y_t \stackrel{P}{\longrightarrow} \mu \quad \text{as } n \to \infty,$$

i.e.  $\bar{Y}_n/n$  converges in probability to  $\mu$  by using inequalities on expectations.